



## ANN Application Of Machine Learning For Evaluating Thermophysical Properties Of Hybrid Nanofluids: A Review

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**Abstract:** The utilization of machine learning methods for modelling the thermophysical properties of hybrid nanofluids has gained substantial attention due to its potential to enhance prediction accuracy and versatility. This study provides all-encompassing analysis of the diverse methods employed in predicting dynamic viscosity and thermal conductivity of hybrid nanofluids. In recent times, intelligence-based models have emerged to predict these essential properties of hybrid nanofluids, therefore artificial neural network is discussed from simple correlation to complex. Optimization algorithm, input factors and training functions significantly influence the reliability of prediction. Furthermore, alternative methodologies like adaptive Neuro-fuzzy inference system and support vector machines are explored. The current review emphasizes the importance of advancing these models by embracing a wider array of input factor and considering novel optimization techniques with the goal of creating predictive models that are both accurate and adaptable across diverse hybrid nanofluid scenarios.

**Keywords:** ANN • Dynamic Viscosity • Hybrid Nanofluids • Machine Learning • Thermal Conductivity

### Introduction:

Nanotechnology offers the potential to enhance system performance and acquire materials with superior attributes in various scientific domains Ramezanizadeh et al (2019). Nanofluids consist of a blend of liquid known as the base fluid and solid nanoparticles in the nano size range and address limitations in heat transfer efficiency observed in conventional heat transfer fluids Mostafa et al (2020). The improved thermophysical properties exhibited by these fluids with their elevated thermal conductivity, position them as the preferred choice for incorporation into heat transfer devices and systems for thermal managements Nazir et al (2019). Despite increased thermal conductivity, the inclusion and settling of solid particles leads to increase in their dynamic viscosity. In general, the thermophysical characteristics of NFs depend on various factors like properties of the base fluid (BF)

concentration, temperature, solid particle shape among others Wang et al (2021).

In prior research, conventional NFs featured an independent material dispersed within the base fluid, similar to conventional nanofluids. Researchers, like Leticia et al. Leticia et al (2019) evaluated thermal conductivity and viscosity within EG-based NFs with diamond/silver nanostructures with temperature and concentration ranges from (10°C-60°C) and (0%-0.1%) respectively. The result showed that the highest thermal conductivity enhancement occurred at 60°C and 0.1% concentration. Trinh et al (2018) explored the impact of temperature on thermal conductivity of graphene-carbon nanotube HNF in ethylene glycol. The result showed that the specified hybrid nanostructure at volume fraction of 0.07% within the BF resulted in significant improvements in thermal conductivity. Asadi (2018) assessed the dynamic viscosity of oil-based nanofluid containing MWCNT/ZnO nanostructure with



temperature range from (15°C-55°C) and concentration from (0.125-1%). They observed that viscosity decreases and improved heat transfer coefficient with increasing temperature.

The experimental measurements of thermal conductivity and dynamic viscosity in HNF is both time-consuming and challenging. To address this, numerous predictive models have been formulated and relying on factors like algorithm choice, input variables and quantity of data points Zendehboudi and Li (2017). Among the assortment of available techniques,

machine learning (ML) approaches have found widespread adoption in domain. Particularly noteworthy the application of artificial neural network (ANN) renowned for their accuracy and precision. Alongside ANN models, other methodologies like support vector machines (SVM) have demonstrated promising capabilities in suggesting NFs properties. The present paper endeavours to provide an all-encompassing review of prior investigations concerning the utilization of ML methods for modelling dynamic viscosity and thermal conductivity in hybrid nanofluids.

### Nomenclature:

|                                                |                                       |
|------------------------------------------------|---------------------------------------|
| ANN: Artificial Neural Network                 | ML: Machine Learning                  |
| ANFIS : Adaptive Neuro-Fuzzy Inferences System | MWCNT: Multi Walled Carbon Nano Tube  |
| BF: Base Fluid                                 | NFs: Nanofluids                       |
| HNF: Hybrid Nanofluid                          | RBF: Radial Basis Function            |
| LSSVM: Least Square Support Vector Machine     | SVM: Support Vector Machines          |
| LS-SVR: Least Square Support Vector Regression | SWCNT: Single Walled Carbon Nano Tube |
| MLP: Multilayer Perceptron                     |                                       |

### Methodology Employed in the Investigation:

To conduct a detailed review, various steps were taken. In step 1: scientific database was undertaken encompassing platforms such as Science Direct, Scopus and Google Scholar. Step 2: Relevant documents were sought using keywords including HNF, Thermal Conductivity, Dynamic Viscosity, ML and

ANN and some methods. Step 3 categorized the advanced collection into studies on thermal conductivity and dynamic viscosity. In step 4: After outlining the article structure including its divisions and subdivisions the collected data from this review was methodically organised and integrated into relevant sections. The overall procedure of this review study is visually depicted in Figure 1.

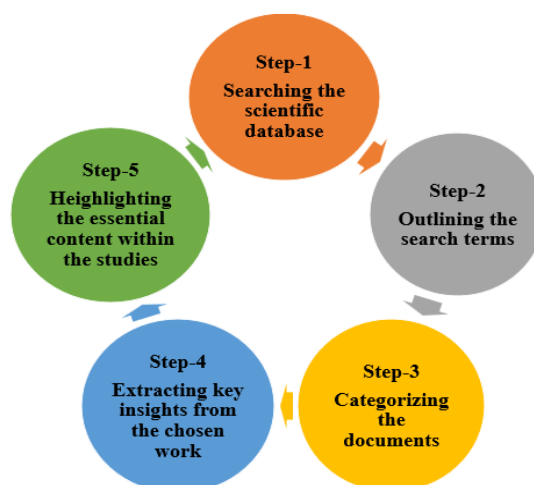


Fig. 1. The Methodology Employed in the Current Review Study



## Most Relevant Methods of Machine Learning:

As previously indicated, there exist numerous machine learning methods for modelling and forecasting the performance of engineering systems Maleki et al (2021). Within this array of methods, the MLP-ANN, ANFIS, LS-SVM and the radial basis Function (RBF) ANN have found extra extensive applications in modelling nanofluid properties. In the ensuing subsections, we explore into those approaches that are most pertinent to the objectives.

### Artificial Neural Network Employing a Multilayer Perceptron Architecture:

The foundation of an ANN is rooted in the amalgamation of intelligent computational techniques with biological systems. Among

$$n_j = \sum_{i=1}^n \omega_{ji} x_i + \theta_j$$

In equation (1),  $k$  represents the count of nodes,  $\theta_j$  denotes the level of the  $j^{\text{th}}$  hidden node and  $\omega_{ji}$  represents the weight of

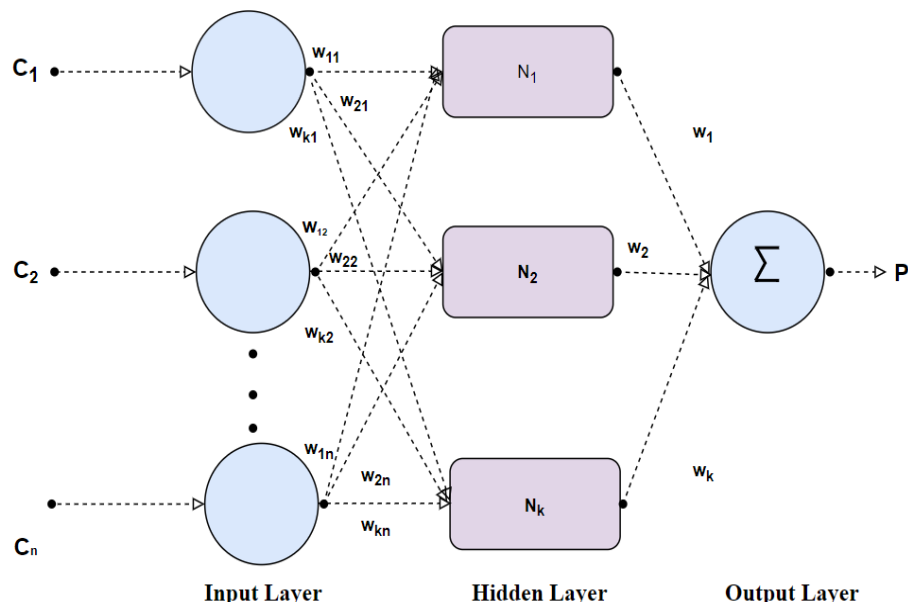
$$y_j = f(n_j) = f\left(\sum_{i=1}^n \omega_{ji} x_i + \theta_j\right)$$

the prominent variations of ANN, the multilayer perceptron (MLP) stands out as one of the most extensively employed. The configuration of MLP is visually elucidated in fig. 1. The MLP consist of nodes across three layers: input, hidden and output. The number of hidden layers can vary based on the problem complexity. Each node employs weight vector to establish connections with nodes in the subsequent layer Zendehboudi and Li (2017). In the networks initial layer, the nodes are added and employed as inputs for the subsequent layer. If we denote the model input as vector  $x$  and  $n_j$  as the input of the  $j^{\text{th}}$  node in the subsequent layer:

$$j = 1, 2, \dots, k \quad (1)$$

connection to that node. Subsequently, the function  $f$  is employed to process and arrange the collective inputs for the subsequent layer leading to:

$$j = 1, 2, \dots, k \quad (2)$$



**Fig. 2. Structure of Multilayer Perceptron-ANN.**

These functions exhibit distinct characteristics and can be joined across various approaches. By scaling the concealed layer output using

linking weight derives node output. The count of inputs corresponds to the number of neurons in the input layer. However,



standardized methodology for determining the size and quantity of hidden layers is absent and they depending on factors like problem intricacy and dataset distribution Panchal et al (2011). As the training process unfolds iteratively neurons are incrementally incorporated to attain an optimal state. In constructing predictive models using MLP, the training phase is crucial and involving bias and weight values adjustments. The widely used backpropagation (BP) algorithm fine-tune bias and weight values during the training phase of MLP, and integral process in constructing neural networks.

#### Modelling Thermal Conductivity Through Machine Learning Approaches:

$$\frac{k_{nf}}{k_{bf}} = 0.006(\varphi^{1.090})T^{1.051} + 1.014$$

(3)

$$\frac{k_{nf}}{k_{bf}} = 4.055 \left( \left( \frac{\varphi}{34} \right)^{1.09} \right) \exp \left( \frac{T}{34} \right) + 1.013$$

(4)

The coefficient of determination for these double correlations at 0.99 respectively. In these equations  $k_{nf}$  represent the thermal conductivity of NFs and  $k_{bf}$  represents the thermal conductivity of BF, while T and  $\varphi$  in equation (3) and (4) indicate the nanofluid temperature and volume fraction. The variable coefficient within the correlations can enhance the comprehensiveness. Rostami et al. Rostami et al (2021) compared the effectiveness of correlations and ANN in predicting the thermal conductivity of CuO-SWCNT/ethylene glycol NF. The result revealed that the highest absolute deviations for correlation and ANN at 5.4% and 0.5% respectively. Visualize in figure 2, the projected values derived from ANN were notably closer to the actual values, underscoring its superiority over correlation. Esfe et al (2017) used both ANNs and correlation techniques to model the thermal conductivity of SWCNT –  $\text{Al}_2\text{O}_3$ /EG nanofluid. The result revealed that ANNs were employed for modelling deviation reduced to 1.93%. Hemmat et al (2018) assessed the

Recent years have seen significant focus on the modelling of thermal conductivity in NFs. Mathematical correlations are favoured for computational efficiency and ease to use, although they may not always provide high accuracy. Akhgar and Toghraie (2018) formulated a relationship to forecast the thermal conductivity of  $\text{TiO}_2$  – MWCNT /  $\text{H}_2\text{O}$  -EG mixtures providing means to approximate thermal conductivity for certain HNF. Within their investigation, they put forward two correlations employing temperature and concentration of solid nanostructures and employed curve fitting to express them as:

reliability of RBF and MPL for modelling the thermal conductivity of HNF comprising MWCNT alongside other oxide particles  $\text{Al}_2\text{O}_3$  and  $\text{TiO}_2$ . They found that the utilization of GMDH yielded the most precise forecasts and achieving coefficient of determination range from (0.96-0.98) depending on the hybrid nanostructure. Shahsavari et al (2025) explored the SVM's superiority over LS-SVR for graphene oxide-silicon carbide/water NFs, while ANFIS offers additional opportunity for precise HNF thermal conductivity.

#### Utilizing Machine Learning Techniques for the Prediction of Dynamic Viscosity:

The dynamic viscosity of NFs significantly impacts on fluid flow dynamics, especially pressure loss and heat transfer capabilities. Understanding its role in influencing reynolds and nusselt number is crucial for addressing thermal engineering issues. Rashmi and Vikash (2020) introduced a correlation derived from the experimental measurements for model the dynamic viscosity of Cu –  $\text{Al}_2\text{O}_3$  –  $\text{TiO}_2$  /  $\text{H}_2\text{O}$  NFs. The



formulated correlation for the NFs was

$$\mu_{nf} = \mu_{bf} \left( 0.955 - 0.00271 * T + 1.858 \frac{\varphi}{100} + \left( 705 \frac{\varphi}{100} \right)^{1.223} \right) \quad (5)$$

Relative to correlations established through curve fitting, the modelling of dynamic viscosity in HNF can achieve greater precision by employing ANN. Amin et al (2021) utilized both LS-SVM and correlation methods predicted dynamic viscosity of HNF with LS-SVM exhibit superior performance due to its improved precision. Notably, R-squared values for the regression outcomes were 0.9

presented in the subsequent manner:

for both correlation and LS-SVM. The graphical representation in Figure 3 demonstrates that the optimized ANN yielded improved agreement between the calculated values and empirically measured results. Notably, the extreme pure deviations were approximately 4.5% and 1.6% when employing correlations and ANN, respectively.

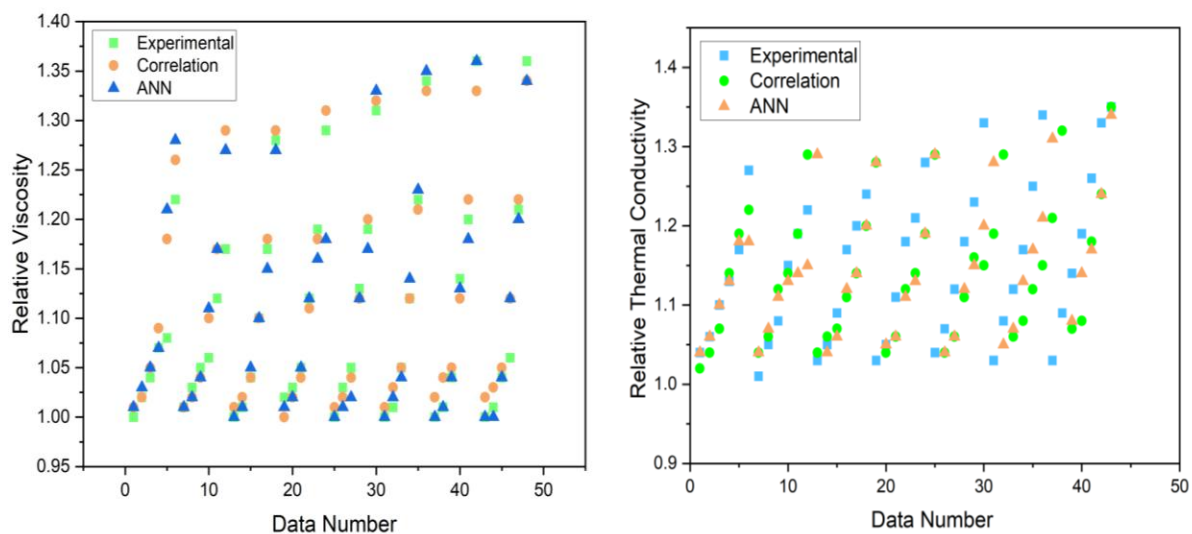


Fig. 3. (a) Comparison between predicted thermal conductivity through correlation and ANN; (b) Comparison between predicted dynamic viscosity through correlation and ANN.

**Conclusion:** This review article focuses on the applications of diverse data-driven techniques for evaluating dynamic viscosity and thermal conductivity in hybrid nanofluids. the principal conclusion distilled from the surveyed literature is outlined as:

- The construction of ANN models and the selection of training and transfer functions play pivotal roles in ensuring the reliability of predictions.
- In additions to ANNs another data-driven method such as ANFIS and SVM exhibit the capability to construct analytical models for properties of HNF.
- Advanced techniques like ANNs exhibit superior predictive capabilities. Also, the Reliability of these models depends on

meticulous architecture design, appropriate training and transfer functions and efficient optimization algorithms.

**Future Recommendations:** The following points outline potential avenues for future advancement in Machine Learning Applications for Modelling Thermophysical Properties of Hybrid Nanofluids

- Expand input variables beyond nanofluids composition to include BF properties, nanostructures attributes and broader experimental data. This expansion will lead to the development of models that are both versatile and highly accurate.



- Explore innovative optimization techniques alongside conventional methods to improve prediction accuracy and minimize errors during network training.
- Investigate the computational efficiency and precision of several training functions in ANN to optimize training processes and enhance model performance.

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